

$$u_p + u_s = d \Rightarrow u_s = d - u_p$$

Minimize: $r^2 = u_p^2 + u_s^2$, with

$$r^2 = u_p^2 + (d - u_p)^2$$

$$r^2 = u_p^2 + d^2 - 2du_p + u_p^2$$

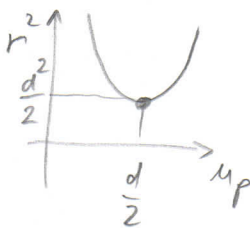
$$r^2 = 2u_p^2 - 2u_p d + d^2$$

$$r^2 = 2 \left[u_p^2 - 2u_p \frac{d}{2} + \frac{d^2}{2} \right]$$

$$r^2 = 2 \left[u_p^2 - 2u_p \frac{d}{2} + \left(\frac{d}{2} \right)^2 + \frac{d^2}{4} \right]$$

$$r^2 = 2 \left[\left(u_p - \frac{d}{2} \right)^2 + \frac{d^2}{4} \right]$$

$r^2 = \text{minimum at } u_p = \frac{d}{2} = u_s$



$$r_{\min}^2 = \frac{d^2}{4} \Rightarrow r_{\min} = \frac{d}{2} = \left(\frac{d}{2} \right) \sqrt{2}$$

as in the above drawing