

$$\Delta G [\cos(\phi - \Delta\phi) - \cos(\phi + \Delta\phi)] = 2d$$

$$d = \frac{\Delta G}{2} 2 \sin\phi \sin\Delta\phi = \Delta G \sin\phi \sin\Delta\phi$$

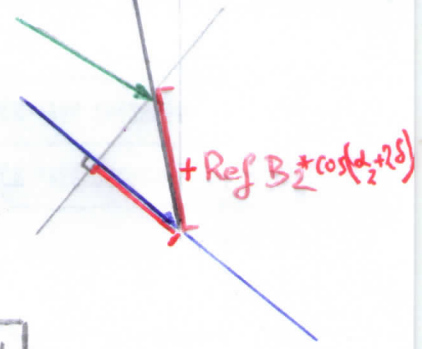
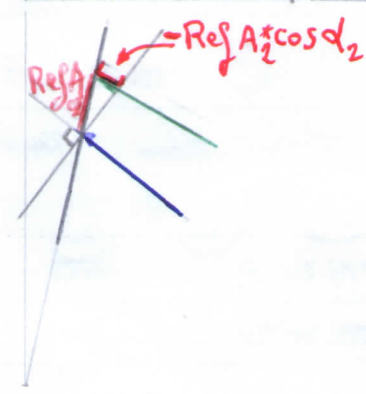
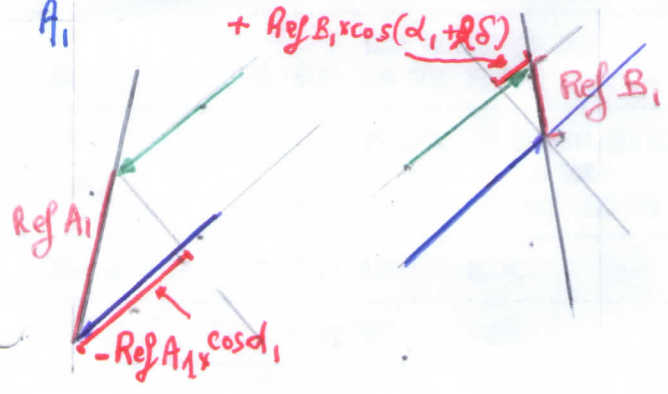
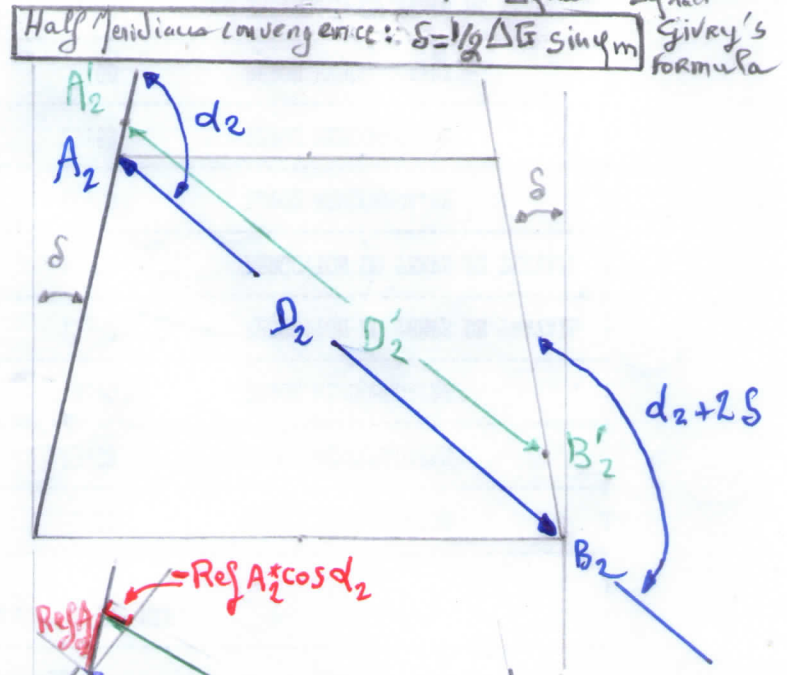
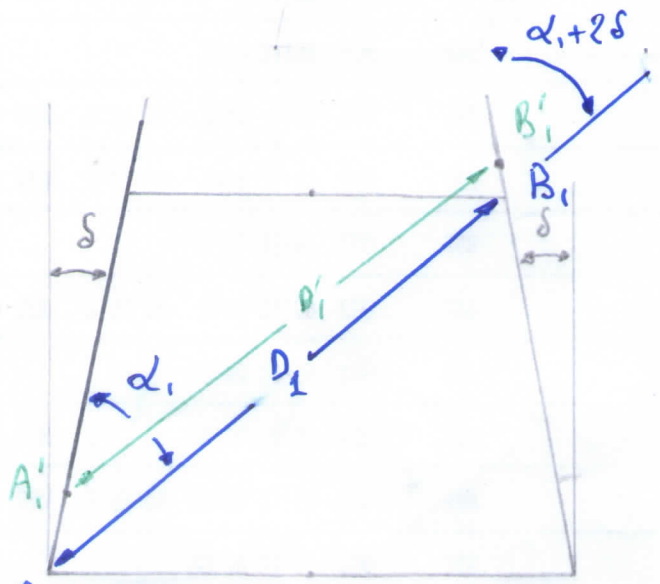
$$\sin\delta = \frac{d}{2\Delta\phi} = \frac{1}{2} \frac{\Delta G \sin\phi \sin\Delta\phi}{\Delta\phi}$$

$$\delta_{\text{rad}} = \delta^{\circ} \times \frac{\pi}{180} \quad \Delta\phi^{\circ} = \frac{\Delta\phi_{\text{rad}} \times 180}{\pi}$$

With δ and $\Delta\phi$ small: $\sin\delta = \delta_{\text{rad}}$ and $\sin\Delta\phi = \frac{\Delta\phi_{\text{rad}}}{1}$. $\sin\delta = \delta_{\text{rad}} = \delta^{\circ} \frac{\pi}{180} = \frac{1}{2} \Delta G^{\circ} \sin\phi \sin\Delta\phi_{\text{rad}} \times \frac{\Delta\phi_{\text{rad}} \times 180}{\pi}$

$$\delta^{\circ} = \frac{1}{2} \Delta G^{\circ} \sin\phi \times \frac{\sin\Delta\phi}{\Delta\phi_{\text{rad}}} \times \frac{\sin\Delta\phi_{\text{rad}}}{\Delta\phi_{\text{rad}}} \approx \frac{1}{2} \Delta G^{\circ} \sin\phi$$

Half Meridians Convergence: $\delta = \frac{1}{2} \Delta G \sin\phi_m$ Givry's formula



From Leftmost Point A to Rightmost Point B:

Formula (1)

$$D' - D = \Delta D = \text{Ref } B \times \cos(d + 2\delta) - \text{Ref } A \times \cos d$$

CONTRACTION OF SMALL ANGULAR DISTANCES DUE TO REFRACTION

NO REFRACTION * 52.64526748 / 134.4488639 WITH REFRACTION * 52.65804802 \leftarrow 52.76404300

(01) \leftarrow 53.01033081 (02) \leftarrow 52.75131149 / 134.8389117 (03) \leftarrow 52.76404300

(04) \leftarrow 52.49229217 (05) \leftarrow 52.69828950

(06) \leftarrow 52.49229217 (07) \leftarrow 52.69828950

(08) \leftarrow 52.49229217 (09) \leftarrow 52.69828950

(10) \leftarrow 52.69828950 (11) \leftarrow 52.69828950

(12) \leftarrow 52.69828950 (13) \leftarrow 52.69828950

(14) \leftarrow 52.69828950 (15) \leftarrow 52.69828950

(16) \leftarrow 52.69828950 (17) \leftarrow 52.69828950

(18) \leftarrow 52.69828950 (19) \leftarrow 52.69828950

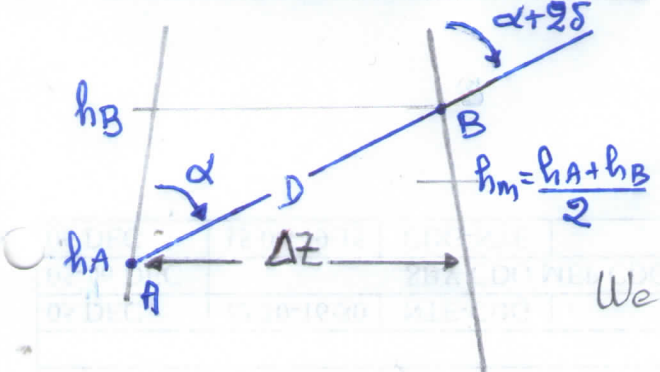
(20) \leftarrow 52.69828950

UNREFRACTED / REFRACTED * DISTANCES / CONTRACTION

- (1) GREAT CIRCLE 0.259070690 / 65.99285161 0.258987600 / 65.99651844 - 0.299124"
- (2) PLANE 0.259071150 / 65.83763047 0.258988052 / 65.84123139 - 0.299154"
- (3) FORMULA (1) (19) * cos((17) + (20)) - (18) cos(17) = -0.298974"

(4) ANOTHER APPROXIMATION

We are given $D, \alpha \& h_A$ (unrefracted)



then (4.1) $h_B = h_A + D \cos \alpha$
 (4.2) $h_m = \frac{1}{2}(h_A + h_B)$
 (4.3) $\Delta Z = D \sin \alpha / \cosh m$
 (4.4) $2\delta = \Delta Z \sin h_m$

We are also assuming that: $(h) > 15^\circ$

(4.5) Ref(h) in arcminutes = $\frac{1}{\tan h}$

Numerical example, same as above:

unrefracted: $D = 0.259070690, \alpha = 65.99285161, E = h_A = 52.64526748$

obtain a contraction of -0.297203"

Other example: Sun, $SD = 32', \alpha = 90^\circ$

HORIZONTAL CONTRACTION

$h = 15^\circ$	-0.5585
$h = 22^\circ$	-0.5585
$h = 30^\circ$	-0.5585
$h = 45^\circ$	-0.5585
$h = 60^\circ$	-0.5585
$h = 75^\circ$	-0.5584

Keen
 27
 October
 2023