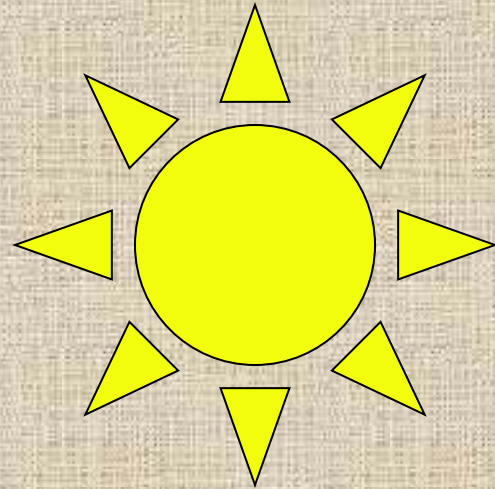


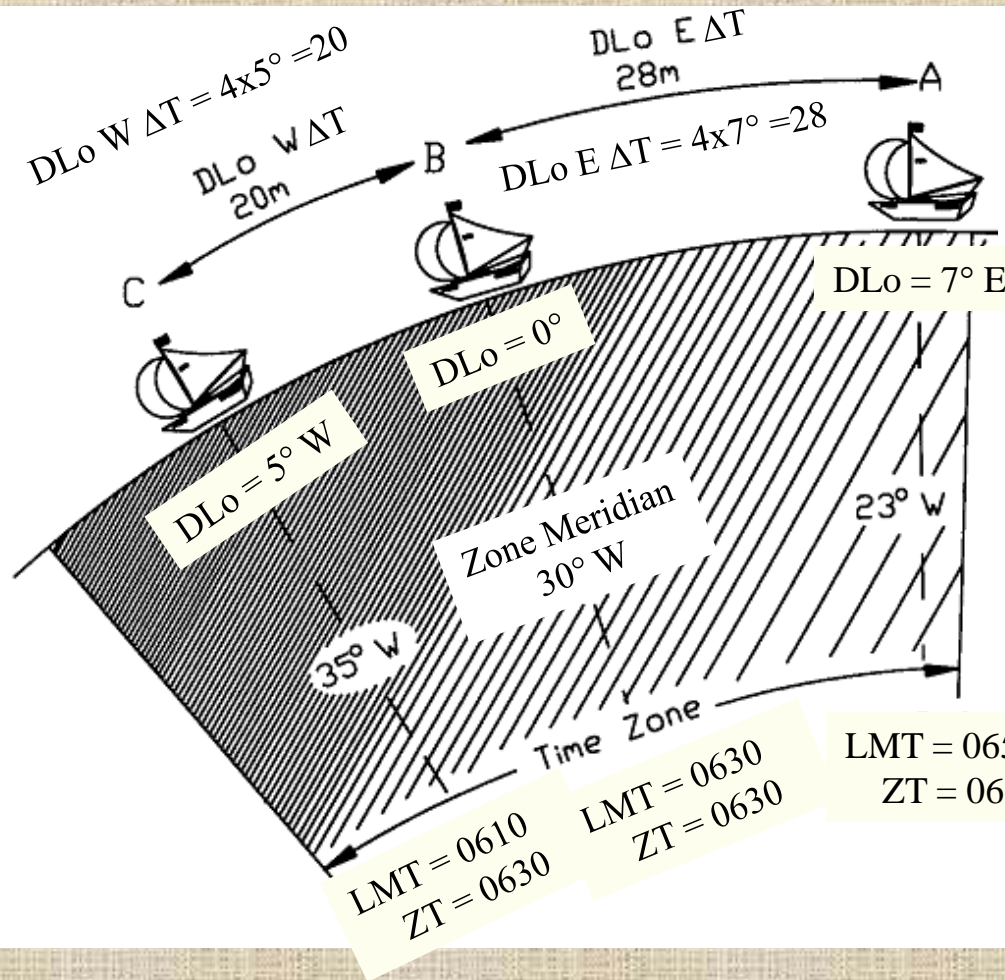
Meridian Transit



Learning Objectives

- Determine Zone Time of Sun's meridian transit using *Nautical Almanac Mer. Pass.* method
- Determine Zone Time of Sun's meridian transit using *Nautical Almanac Eqn. of Time* method
- Determine Zone Time of Sun's meridian transit using **GHA = Observer's Meridian** method
This method is required for homework & test
- Understand difference between Zone Time (**ZT**) and Local Mean Time (**LMT**)
- Determine latitude from an observation of the Sun at meridian transit

Zone Time (ZT) and Local Mean Time (LMT)



Determining Local Mean Time (LMT) From Zone Time (ZT)

Recall that The Sun moves West at a rate of 15 degrees of Longitude per hour of time or 4 minutes of time per degree of Longitude

$$LMT = ZT - DLo\ W$$

$$LMT = ZT + DLo\ E$$

Meridian Transit of Sun

- **GHA** – defines position of apparent Sun
- Meridian Transit – apparent Sun crosses observer's meridian
- **Local Hour Angle (LHA) = $0^{\circ} 00.0'$**
GHA = Observer's Meridian
- **Local Apparent Time (LAT) = 12-00-00**
- Meridian Transit of Sun is also known as **Local Apparent Noon (LAN)**

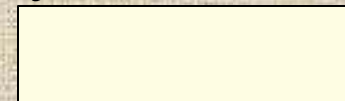
Mean Sun & Apparent Sun

- **Mean Sun** - an imaginary Sun
invented for keeping Zone Time
- **Apparent Sun** - the observable Sun
determines Apparent Time
- Difference is *Equation of Time*
- Meridian Transit occurs at high noon
12 hours Local Apparent Time (**LAT**)
A Sun Dial displays Local Apparent Time

Meridian Passage & Equation of Time

The *Equation of Time* listed in the *Nautical Almanac* tabulates the difference between the apparent Sun and mean Sun.

If meridian passage at Greenwich is earlier than 1200 GMT then the apparent Sun is ahead of the mean Sun and the *Equation of Time* is positive and is shown without a shaded background.



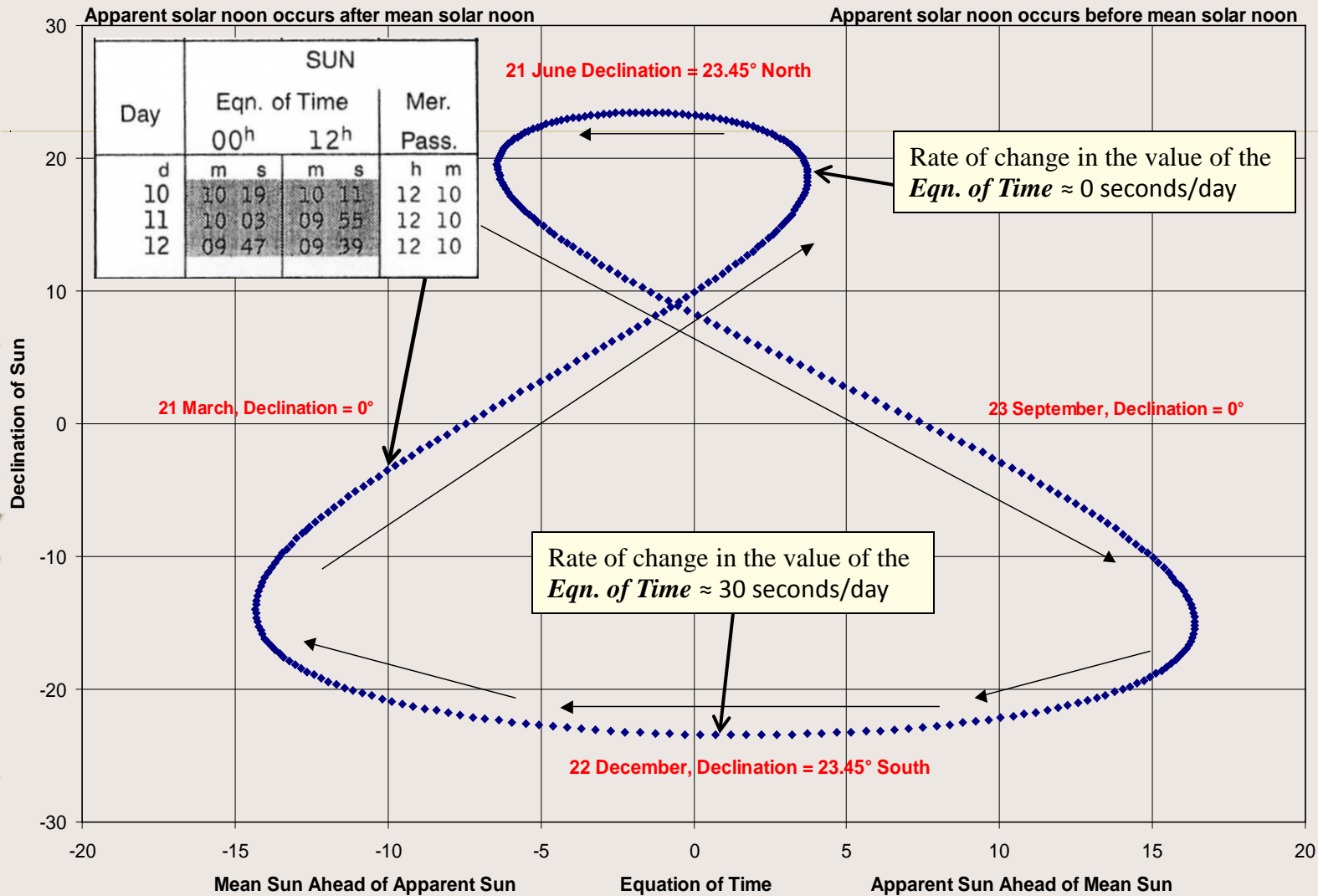
If meridian passage at Greenwich is later than 1200 GMT then the mean Sun is ahead of the apparent Sun and the *Equation of Time* is negative and is shown within a gray shaded background.



| Day | SUN | | | | | |
|-----|-----------------|----|-----------------|----|------------|----|
| | Eqn. of Time | | | | Mer. Pass. | |
| | 00 ^h | | 12 ^h | | | |
| d | m | s | m | s | h | m |
| 10 | 10 | 19 | 10 | 11 | 12 | 10 |
| 11 | 10 | 03 | 09 | 55 | 12 | 10 |
| 12 | 09 | 47 | 09 | 39 | 12 | 10 |

The time of the Sun's meridian passage listed in the *Nautical Almanac* is the GMT of the Sun's passage over the prime meridian at Greenwich rounded to the nearest whole minute.

Analemma



The Nautical Almanac Values Shown In Gray Box

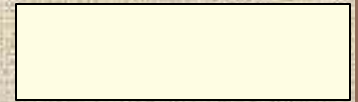
The Nautical Almanac Values Shown In White Box

Apparent Time

If the apparent Sun is ahead of the mean Sun

then: $LAT = LMT + Eqn. of Time$

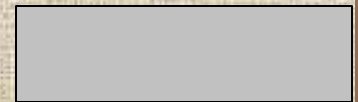
$LMT = LAT - Eqn. of Time$



If the mean Sun is ahead of the apparent Sun

then: $LAT = LMT - Eqn. of Time$

$LMT = LAT + Eqn. of Time$



Transit via *Nautical Almanac* Mer. Pass.

On 22 December 2014 you plan on taking a meridian transit sight of the sun from Ediz Hook, $L = 48^{\circ} 08.5' N$; $Lo = 123^{\circ} 26.1' W$; (ZD +8)

From the *Nautical Almanac* you determine that on 22 December 2014 meridian passage at the Greenwich meridian occurs at 1159 GMT.

Assume[†] meridian passage at your Zone Meridian of $120^{\circ} W$ also occurs at 1159 Zone Time. Your DLo is $3^{\circ} 26.1' W$ which equates to 13 minutes 44 seconds. You can now calculate meridian passage at Ediz Hook on 22 December 2014

Zone Time of Meridian Passage @ $120^{\circ}W$ 11-59-00

DLo West ΔT + 13-44

Zone Time of Meridian Passage @ $123^{\circ} 26.1'W$ 12-12-44

Maximum error less than 30 seconds

| Day | Sun | | | | Mer. Pass. |
|-----|---------------------------|----|-----|----|------------|
| | <i>Eqn of Time</i> 00h | | 12h | | |
| d | m | s | m | s | h m |
| 21 | 02 | 13 | 01 | 58 | 11 58 |
| 22 | 01 | 43 | 01 | 28 | 11 59 |
| 23 | 01 | 13 | 00 | 58 | 11 59 |

[†] Accuracy is degraded by rounding time of Mer. Pass. to a whole minute and the change in the value of the *Eqn. of Time* between 1200 GMT & 1200 LAT at observer's meridian. Accuracy could be improved by using 11:58:32 as mer. Pass. time. (See Analemma)

Transit via *Nautical Almanac Eqn. of Time*

On 22 December 2014 you plan on taking a meridian transit sight of the sun from Ediz Hook, $L = 48^{\circ} 08.5' N$; $Lo = 123^{\circ} 26.1' W$; (ZD +8)

From the *Nautical Almanac* you determine that on 22 December 2014 *Eqn. of Time* at 1200 GMT is 1 minute 28 seconds. Apparent Sun is ahead of the Mean Sun. Meridian passage at your Zone Meridian will be at 1200 LAT. Since your is Zone Meridian is $120^{\circ}W$ your DLo is $3^{\circ} 26.1'W$ which equates to 13 minutes 44 seconds.

Using 01 min 28 seconds as the value of the *Eqn. of Time*, determine meridian passage at Ediz Hook on 22 December 2014

Maximum error[†] is less than 15 seconds
 Accuracy varies through the year from ≈ 1 to ≈ 15 seconds, depending on the rate of change in the *Eqn. of Time* (See Analemma)

| | |
|------------------------------------|----------|
| Noon LAT | 12-00-00 |
| Eqn. of Time | - 01-28 |
| LMT | 11-58-32 |
| DLo of $3^{\circ} 26.1'W \Delta T$ | + 13-44 |
| Zone Time | 12-12-16 |

| Day | Sun | | | | Mer. Pass. | |
|-----|--------------|-----|-------|----|------------|--|
| | Eqn. of Time | | 12h | | | |
| | d | m s | m s | h | m | |
| 21 | 02 | 13 | 01 58 | 11 | 58 | |
| 22 | 01 | 43 | 01 28 | 11 | 59 | |
| 23 | 01 | 13 | 00 58 | 11 | 59 | |

[†] Accuracy is degraded by the change in the value of the *Eqn. of Time* between 1200 GMT & 1200 LAT at observer's meridian. (See Analemma)

Determining UT for GHA = LHA

If you are West of Greenwich, select the latest UT hour from the *Nautical Almanac* where GHA is less than your meridian.

If you are East of Greenwich, select the latest UT hour from the *Nautical Almanac* where GHA is less than 360° minus your meridian.

Take difference between your meridian and the above GHA

Go to the *Yellow Pages* and determine the minutes and seconds that correspond to the above difference.

The Time of Meridian Passage is the above UT hour + the minutes and seconds you determined from the *Yellow Pages*.

At Meridian Passage the LHA of the Sun = $0^\circ 0.0'$

GHA of the Sun is equal to the observer's meridian

Transit via $GHA = \text{Observer's Meridian}$

On 22 December 2014 you plan on taking a meridian transit sight of the sun from Ediz Hook, $L = 48^{\circ} 08.5' \text{ N}$; $Lo = 123^{\circ} 26.1' \text{ W}$; (ZD +8)

From the *Nautical Almanac* you determine that at UT 2000 the GHA of the Sun will be $120^{\circ} 19.4'$ with a Declination of $23^{\circ} 25.9' \text{ S}$

Then the Difference between $123^{\circ} 26.1'$ and $120^{\circ} 19.4'$ is $03^{\circ} 06.7'$

From the yellow pages we find that $03^{\circ} 06.7'$ converted to time is 12 minutes 27 seconds

| | |
|---|-----------------|
| GHA of the Sun = $120^{\circ} 19.4'$ @ UT | 20-00-00 |
| $3^{\circ} 26.1'$ converted to time | <u>+ 12-27</u> |
| GHA of the Sun = $120^{\circ} 26.1'$ @ UT | 20-12-27 |
| ZD | <u>+8 (rev)</u> |
| Zone Time of meridian transit | 12-12-27 |

Accuracy ± 1 second

Comparison of Methods

- The rate of change in the value of the *Eqn. of Time* is at its maximum value on 22 December (≈ 30 seconds/day)

- *Nautical Almanac Mer. Pass. method*

Zone Time of 12-12-44 $H_c = 18^\circ 25.61'$

- *Nautical Almanac Eqn. of Time method*

Zone Time of 12-12-16 $H_c = 18^\circ 25.61'$

- GHA = Observer's Meridian method

Zone Time of 12-12-27 $H_c = 18^\circ 25.61'$

- For Zone Time of 12-10-45 $H_c = 18^\circ 25.55'$

No significant change in H_c over this time period

- For Zone Time of 12-13-55 $H_c = 18^\circ 25.56'$

Skill 1 – Find Time of Transit

On 29 February you plan on taking a meridian transit sight of the sun from Ediz Hook, $L = 48^{\circ} 08.5' N$; $Lo = 123^{\circ} 26.1' W$; (ZD +8).

Use Excerpts from *Nautical Almanac* supplied with JN Student Manual to determine Zone Time of meridian transit using the three methods shown below:

- *Nautical Almanac* Mer. Pass. method
- *Nautical Almanac* Eqn. of Time method
- GHA = Observer's Meridian method

Also compute Hc for each of the above meridian transit times.

Nautical Almanac Mer. Pass. method

On 29 February you plan on taking a meridian transit sight of the sun from Ediz Hook, L = 48° 08.5' N; Lo 123° 26.1' W; (ZD +8).

Use Excerpts from *Nautical Almanac* supplied with JN course materials to find Zone Time of Transit.

Your DLo is 3° 26.1'W which equates to 13 minutes 44 seconds.

Zone Time of Meridian Passage @ 120°W 12-13-00

DLo West ΔT + 13-44

Zone Time of Meridian Passage @ 123° 26.1'W 12-26-44

LHA 0.00000

Lat 48.14167

Dec -7.68367

Zn = 180°

Hc = 34° 10.48'

| Day | Sun | | | | Mer. Pass. |
|-----|--------------------|----|-----|----|---------------|
| | Eqn of Time 00h | | 12h | | |
| d | m | s | m | s | h m |
| 27 | 13 | 01 | 12 | 56 | 12 13 |
| 28 | 12 | 51 | 12 | 45 | 12 13 |
| 29 | 12 | 40 | 12 | 34 | 12 13 |

Nautical Almanac Eqn. of Time method

On 29 February you plan on taking a meridian transit sight of the sun from Ediz Hook, L = 48° 08.5' N; Lo 123° 26.1' W; (ZD +8).

Use Excerpts from *Nautical Almanac* supplied with JN course materials to find Zone Time of Transit.

Eqn. of Time @ 12 hours GMT is 12 min 34 seconds

The mean sun is ahead of the apparent sun

Your DLo is 3° 26.1'W which equates to 13 minutes 44 seconds.

LHA 0.00000
 Lat 48.14167
 Dec -7.68367

Noon LAT 12-00-00
Eqn. of Time + 12-34
 LMT 12-12-34
 DLo of 3° 26.1'W ΔT + 13-44
 Zone Time 12-26-18

Zn = 180° Hc = 34° 10.48'

| Day | Sun | | Mer. Pass. | |
|-----|--------------------|-----|------------|----|
| | <i>Eqn of Time</i> | | | |
| | 00h | 12h | | |
| d | m | s | m | s |
| 27 | 13 | 01 | 12 | 56 |
| 28 | 12 | 51 | 12 | 45 |
| 29 | 12 | 40 | 12 | 34 |

GHA = Observer's Meridian method

On 29 February you plan on taking a meridian transit sight of the sun from Ediz Hook, L = 48° 08.5' N; Lo 123° 26.1' W; (ZD +8).

Use Excerpts from *Nautical Almanac* supplied with JN course materials to find Zone Time of Transit.

From the *Nautical Almanac* you determine that at UT 2000 the GHA of the Sun will be 116 ° 52.5' with a Declination of 07° 41.4'S

Then the Difference between 123° 26.1' and 116 ° 52.5' is 06° 33.6'

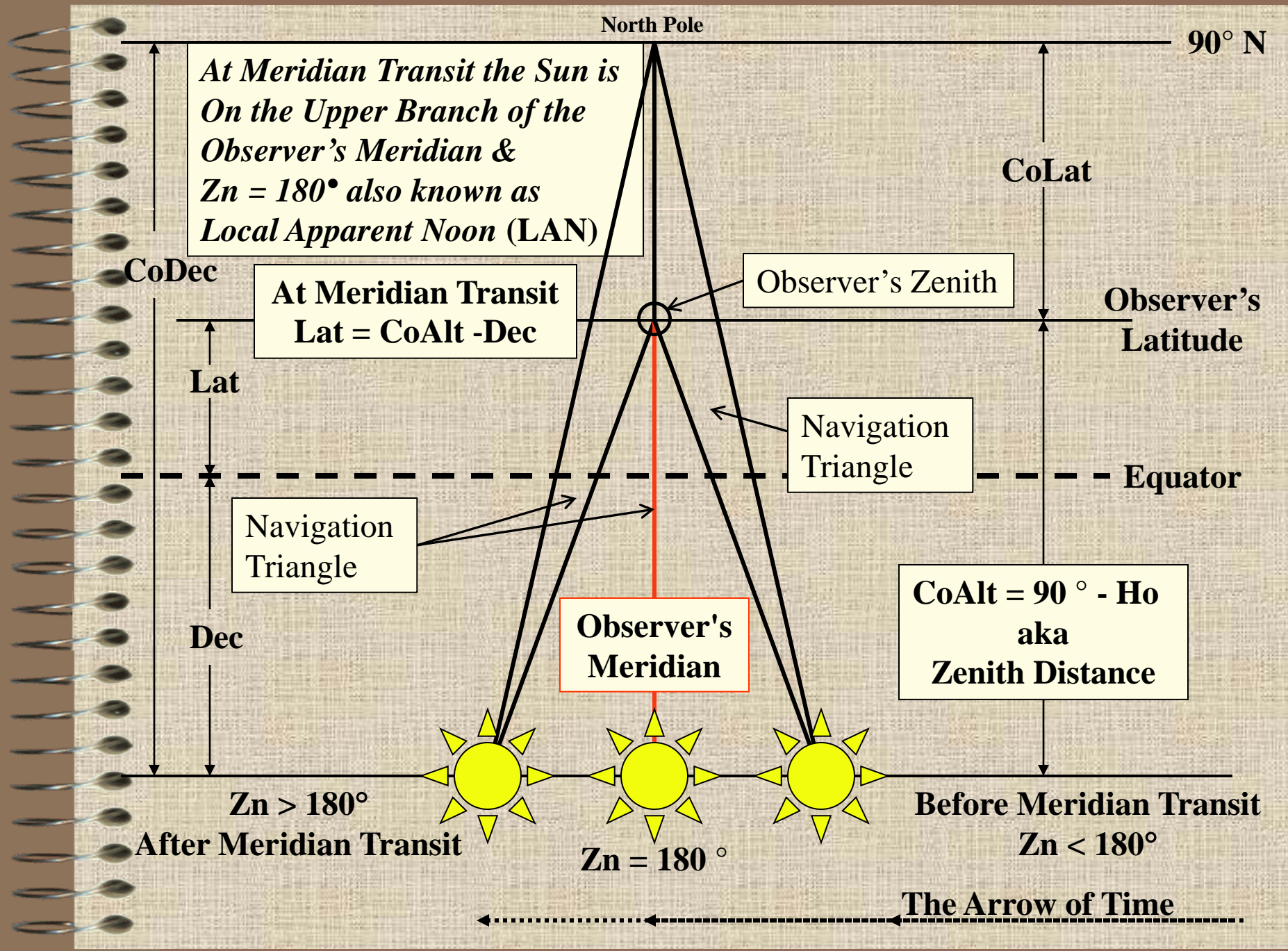
From the yellow pages we find that 06° 33.6' converted to time is 26 minutes 14 seconds

| | | | |
|-----|-----------------|-----------------------------|-----------------|
| | | UT | 20-00-00 |
| | | 06° 33.6' converted to time | <u>+ 26-14</u> |
| | | UT | 20-26-14 |
| | | ZD | <u>+8 (rev)</u> |
| | | Zone Time | 12-26-14 |
| LHA | <u>0.00000</u> | Zn = 180° | Hc = 34° 10.48' |
| Lat | <u>48.14167</u> | | |
| Dec | <u>-7.68367</u> | | |

Computing Latitude

- Obtain Ho at Time of Transit
- Subtract Ho from 90° to obtain CoAlt
- Name of CoAlt is direction from the body to the observer
- For GMT of the sight, obtain Dec of sun from the *Nautical Almanac*
- Combine CoAlt and Dec to obtain your latitude: $\text{Lat} = \text{CoAlt} \pm \text{Dec}$

If CoAlt & Dec have same name add; If opposite names subtract



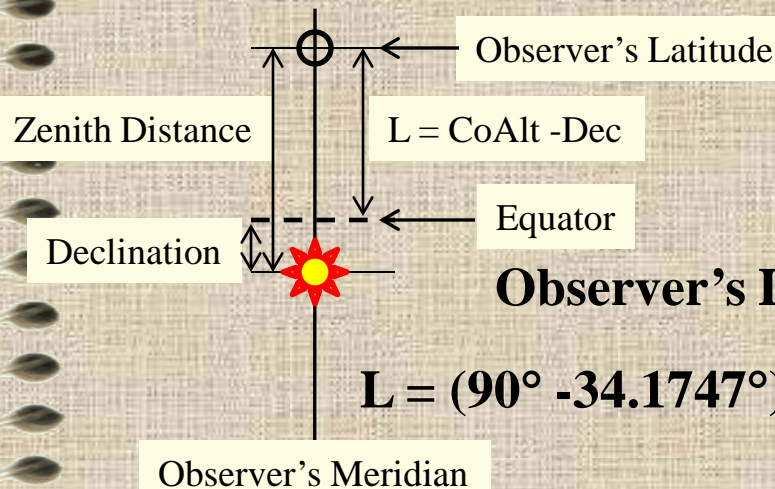
Skill 1 – Solutions Comparison

**29 February meridian transit sight of the sun from Ediz Hook,
L 48° 08.5' N Lo123° 26.1' W (ZD +8).**

■ *Nautical Almanac Mer. Pass. Method* **Zone Time 12-26-44**
Hc = 34° 10.48'

■ *Nautical Almanac Eqn. of Time method* **Zone Time 12-26-18**
Hc = 34° 10.48'

■ **GHA = Observer's Meridian method** **Zone Time 12-26-14**
Hc = 34° 10.48'



Declination of Sun 07° 41.0' S = 7.690°

Observer's Latitude = Zenith Distance ± Declination

$L = (90^\circ - 34.1747^\circ)N - 7.6833^\circ S = 48.137^\circ N = 48^\circ 08.5' N$

Example - Computing Latitude

Observer North of Equator and also North of Sun

$$H_o = 70^\circ$$

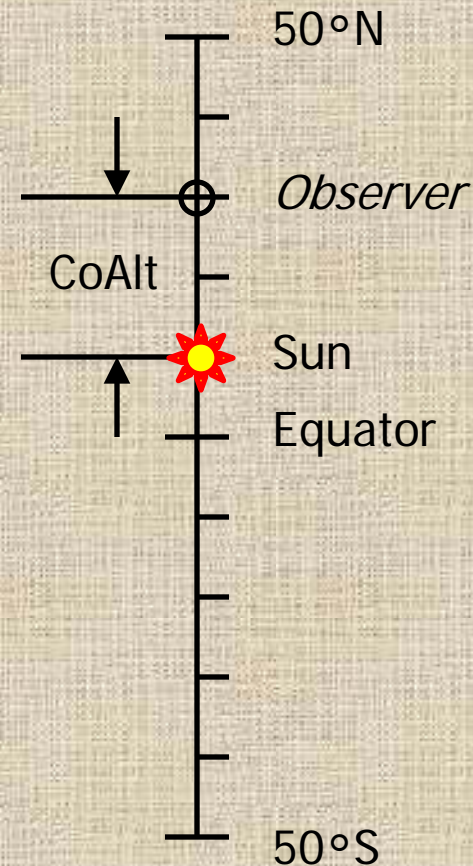
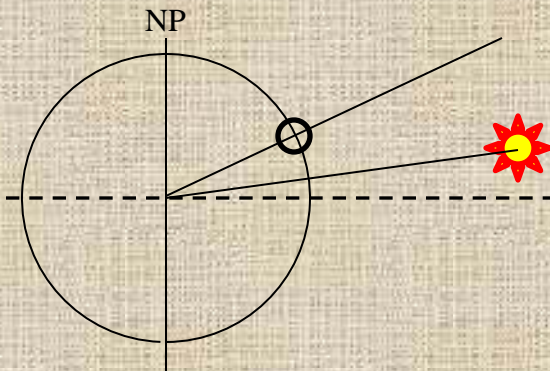
$$Z_n = 180^\circ$$

$$\text{CoAlt} = 90^\circ - 70^\circ = 20^\circ \text{ N}$$

$$\text{Dec} = 10^\circ \text{ N}$$

$$L = \text{CoAlt} \pm \text{Dec}$$

$$L = 20^\circ \text{ N} + 10^\circ \text{ N} = 30^\circ \text{ N}$$



Example - Computing Latitude

Observer North of Equator but South of Sun

$$H_o = 80^\circ$$

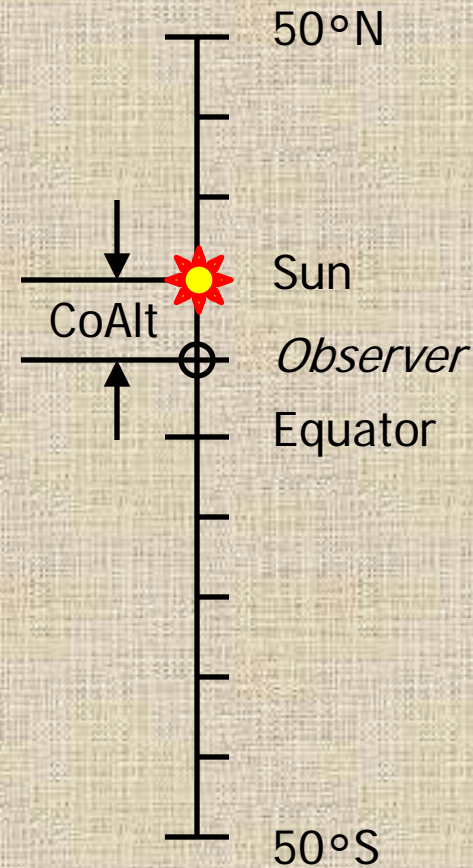
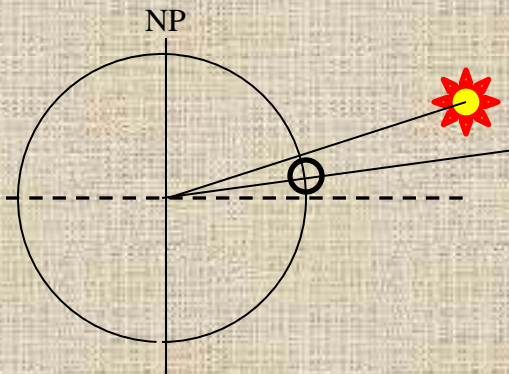
$$Z_n = 360^\circ$$

$$\text{CoAlt} = 90^\circ - 80^\circ = 10^\circ \text{ S}$$

$$\text{Dec} = 20^\circ \text{ N}$$

$$L = \text{CoAlt} \pm \text{Dec}$$

$$L = 10^\circ \text{ S} - 20^\circ \text{ N} = 10^\circ \text{ N}$$



Example - Computing Latitude

Observer South of Equator & also South of Sun

$$H_o = 30^\circ$$

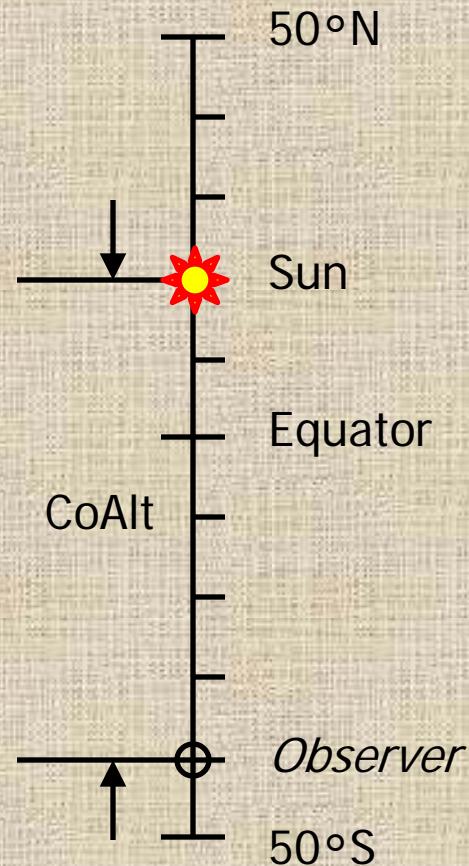
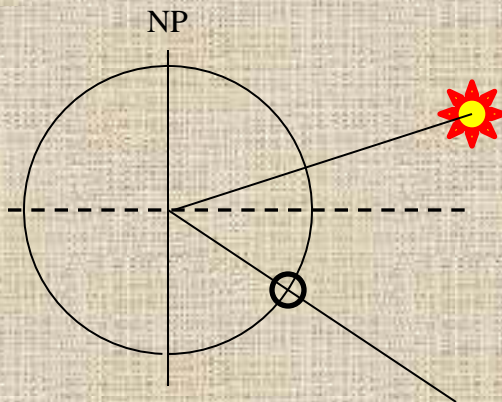
$$Z_n = 360^\circ$$

$$\text{CoAlt} = 90^\circ - 30^\circ = 60^\circ \text{ S}$$

$$\text{Dec} = 20^\circ \text{ N}$$

$$L = \text{CoAlt} \pm \text{Dec}$$

$$L = 60^\circ \text{ S} - 20^\circ \text{ N} = 40^\circ \text{ S}$$



LATITUDE BY MERIDIAN TRANSIT

| | | | |
|--|--------------|-----------------------|------------------|
| | 90° | <u>89° 60'</u> | |
| | - Ho | _____ ° _____' | |
| CoAlt = 90° - Ho | | _____ ° _____' | N / S * |
| | Dec | _____ ° _____' | N / S |
| Δ = CoAlt ± Dec | | _____ ° _____' | N / S ** |
| If (Δ > 90°) then Δ = 180° - Δ | | _____ ° _____' | N / S *** |
| | L = Δ | _____ ° _____' | N / S |
| | DR L | _____ ° _____' | N / S |
| | a | _____ | nm |

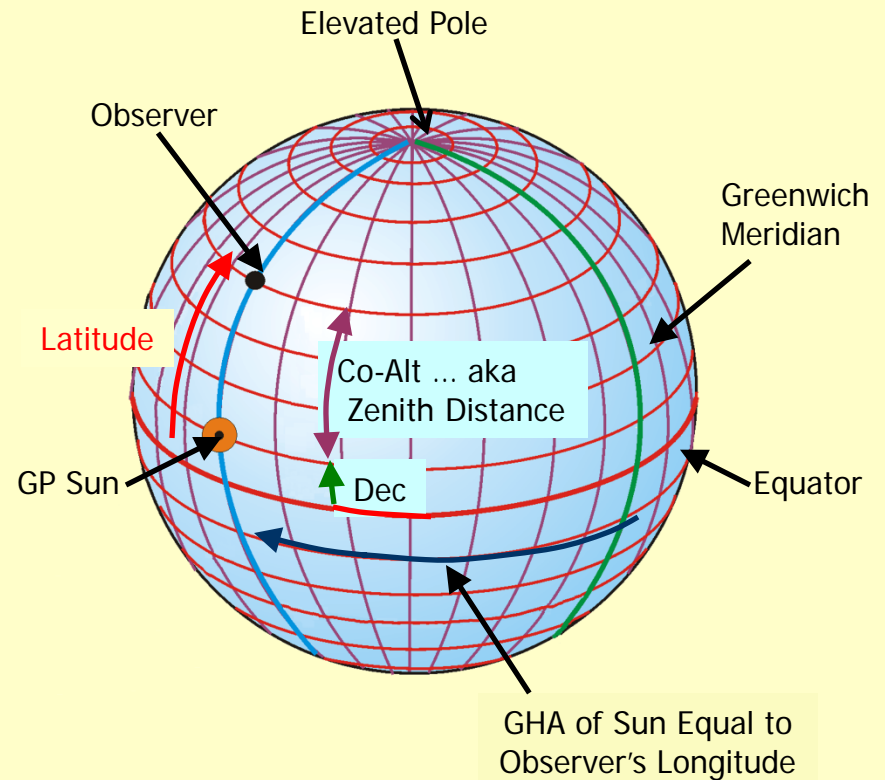
- * CoAlt name is same as direction from the body's declination to your DR Latitude
- ** If CoAlt and Dec have same name, add.
- ** If CoAlt and Dec have opposite names, subtract.
- *** If Δ > 90° body is on lower branch of your meridian

Reviewing -- Meridian Transit

Celestial body is on the upper branch of observer's meridian

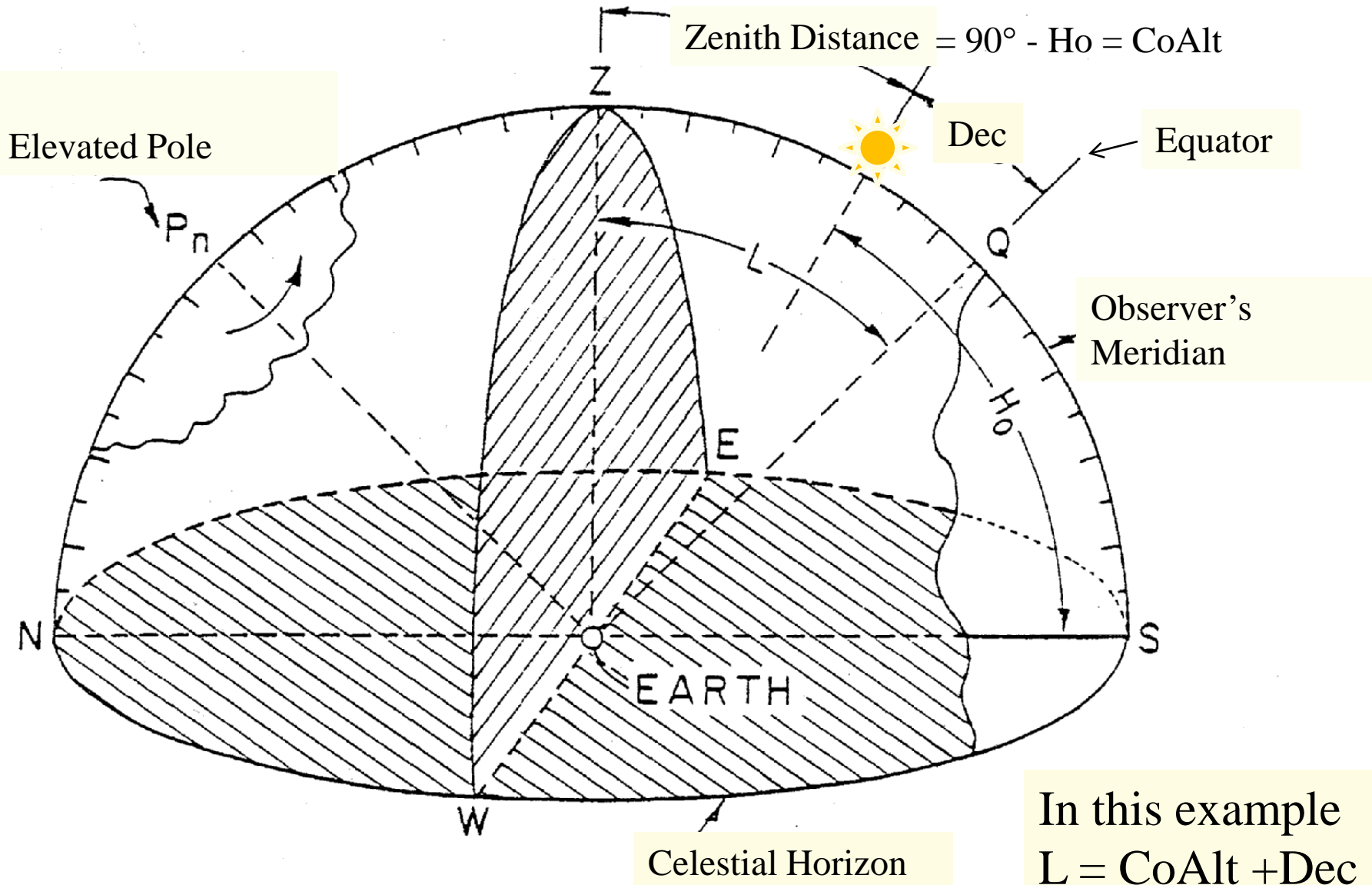
- LHA of Sun = $000^{\circ} 00.0'$
- Sun reaches max. altitude for that date & reference position.
- Azimuth of body is 0° (due north) or (180°) due south of observer's position.
- Navigation triangle collapses to straight line
 - Elevated pole, observer, and GP of body are all on the observer's meridian.
 - Observer's latitude can be found by simple addition or subtraction

Local Apparent Time = 1200



Observer's latitude = Zenith Distance \pm Declination of Sun

Isometric of Meridian Transit Diagram

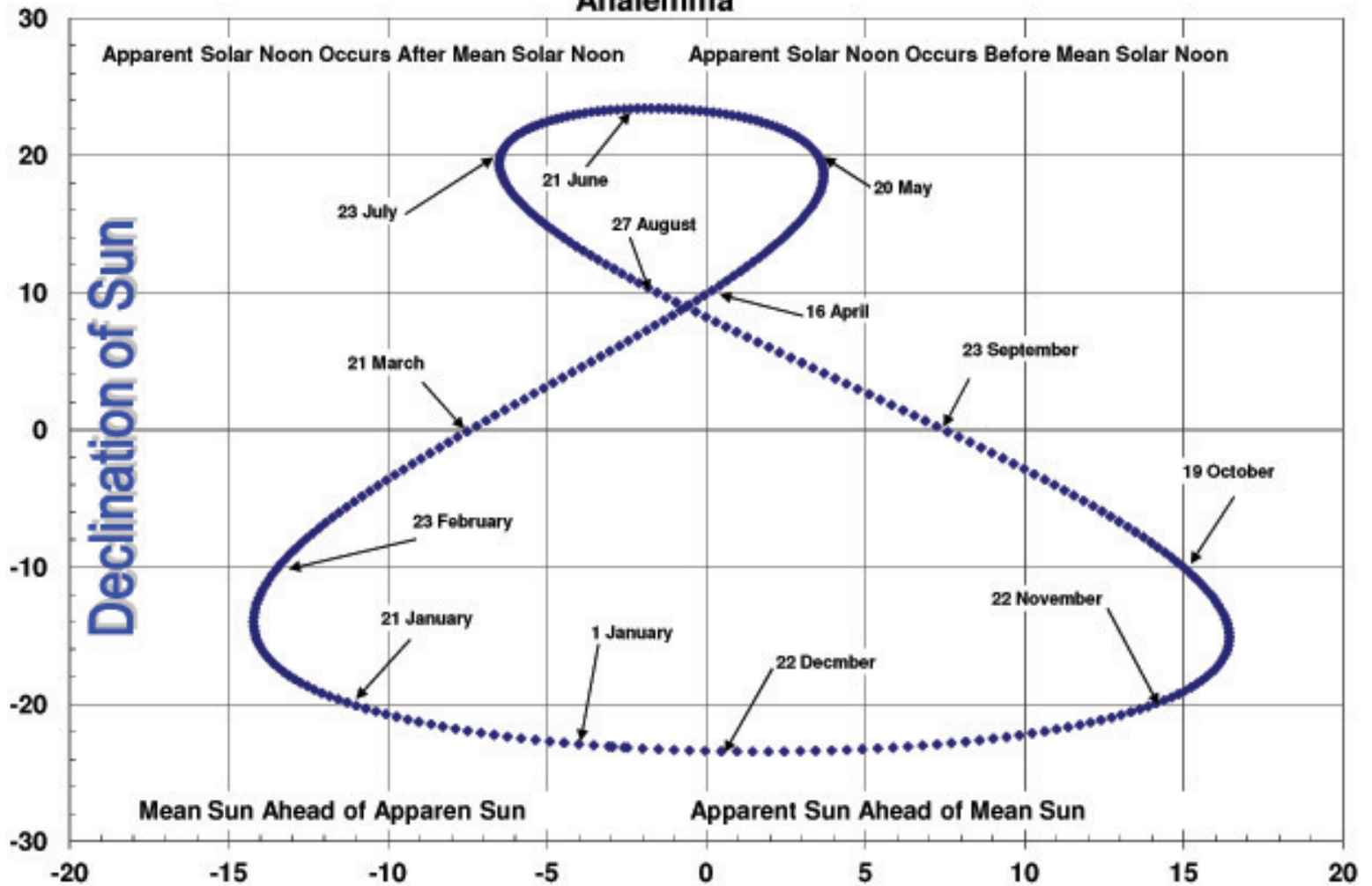


Altitude of Sun at Transit for Year 2003

Location 48° 8.5' N 123° 26.0' W

| Date | Sun's Altitude @ Transit | Sun's Altitude @ Transit ± 60 Seconds |
|--------------|--------------------------|---------------------------------------|
| 15 January | 21° 46.54' | 21° 46.52' |
| 15 February | 29° 15.43' | 29° 15.42' |
| 15 March | 39° 48.38' | 39° 48.37' |
| 15 April | 51° 41.97' | 51° 41.95' |
| 15 May | 61° 27.25' | 61° 27.20' |
| 15 June | 65° 10.57' | 65° 10.52' |
| 15 July | 63° 20.93' | 63° 20.88' |
| 15 August | 55° 50.60' | 55° 50.55' |
| 15 September | 44° 48.49' | 44° 48.44' |
| 15 October | 33° 16.31' | 33° 16.30' |
| 15 November | 23° 19.64' | 23° 19.60' |
| 15 December | 18° 34.88' | 18° 34.86' |

Analemma



Declination of Sun

Equation of Time