

Longhand Haversine Sight Reduction

B = Latitude

dec = Declination

t = Meridian Angle

$$\text{Haversine } hv(x) = \sin^2(x/2) = (1 - \cos(x))/2$$

$$\text{Inverse haversine } hv^{-1}(x) = 2 * \text{asin}(\sqrt{x})$$

Altitude

By computation

ZD = Zenith Distance

Hc = (90 - ZD) Calculated Altitude

$$hv(ZD) = n + (1 - (n + m)) * a$$

Same Name

$$n = hv(B - \text{dec})$$

$$m = hv(B + \text{dec})$$

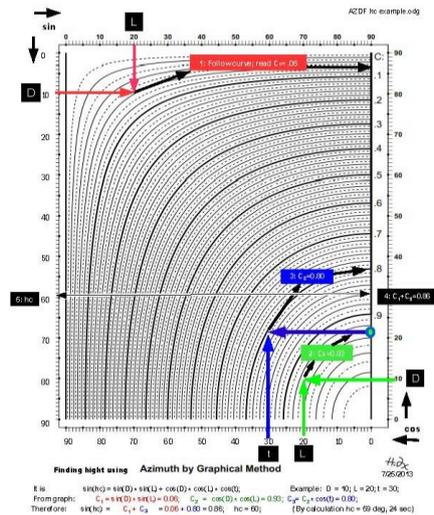
Contrary Name

$$n = hv(B + \text{dec})$$

$$m = hv(B - \text{dec})$$

$$a = hv(t)$$

By Hanno azimuth diagram



Azimuth

By computation

$$hv(Z) = (a - n) / (1 - (n + m))$$

Same Name

$$a = hv(90^\circ - \text{dec})$$

Contrary Name

$$a = hv(90^\circ + \text{dec})$$

$$m = hv(B + Hc)$$

$$n = hv(B - Hc)$$

N Latitude:

$$\text{If LHA} > 180^\circ, Z_n = Z$$

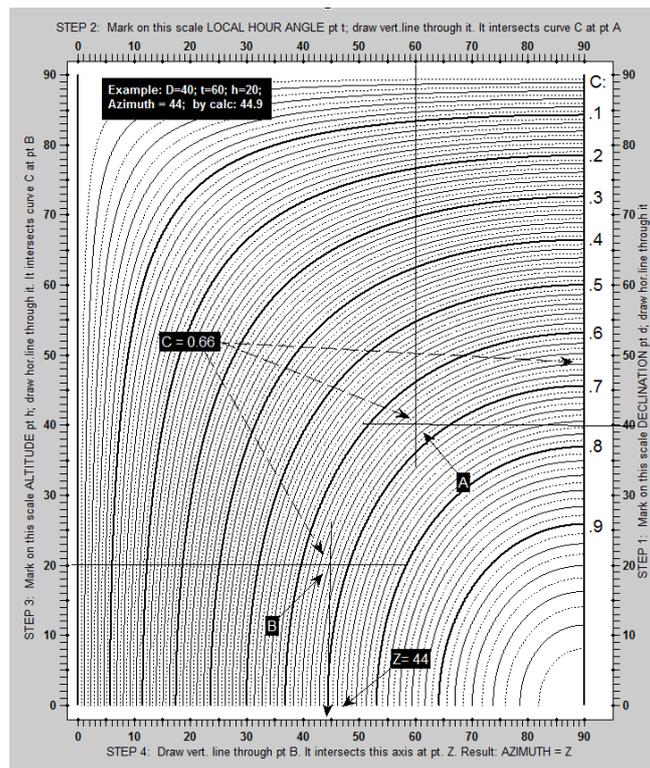
$$\text{if LHA} < 180^\circ, Z_n = 360^\circ - Z$$

S Latitude:

$$\text{If LHA} > 180^\circ, Z_n = 180^\circ - Z$$

$$\text{if LHA} < 180^\circ, Z_n = 180^\circ + Z$$

By Hanno azimuth diagram



$$\sin Z \cos Hc = \sin t \cos \text{dec}$$