

GREAT CIRCLE PLANNING

Given:

- ★ L_1 = Departure Latitude N and W = +
- ★ L_2 = Destination Latitude S and E = -
- λ_1 = Departure Longitude
- λ_2 = Destination Longitude Δt = time between positions
- L_i = Intermediate Latitude
- λ_i = Intermediate Longitude
- H_i = Initial True Heading
- D = Distance in Nautical Miles
- H = Heading Angle
- $D = 60 \cos^{-1} [\sin L_1 \sin L_2 + \cos L_1 \cos L_2 \cos (\lambda_2 - \lambda_1)]$

$$H = \cos^{-1} \left[\frac{\sin L_2 - \sin L_1 \cos (D/60)}{\sin (D/60) \cos L_1} \right]$$

$$H_i = H \text{ if } \sin (\lambda_2 - \lambda_1) < 0$$

$$= 360 - H \text{ if } \sin (\lambda_2 - \lambda_1) \geq 0$$

Given (L_1, λ_1) , (L_2, λ_2) and λ_i —the following formula computes the latitude of L_i where λ_i intersects the great circle defined by (L_1, λ_1) and (L_2, λ_2) .

$$L_i = \tan^{-1} \left[\frac{\tan L_2 \sin (\lambda_i - \lambda_1) - \tan L_1 \sin (\lambda_i - \lambda_2)}{\sin (\lambda_2 - \lambda_1)} \right]$$

(This formula can be very useful when matching charts of different projections or scales.)

RHUMB LINE PLANNING

Given:

- Δt = time between positions
- L_1 Dept Lat
- L_2 Dest Lat
- λ_1 Dept Long

- λ_2 Dest Long
- C = Rhumb line True Course
- D = Rhumb line Distance
- π = Pi (3.14159....)

$$C = \tan^{-1} \left[\frac{\pi (\lambda_1 - \lambda_2)}{180 (\ln \tan (45 + 1/2 L_2) - \ln \tan (45 + 1/2 L_1))} \right]$$

$$D = \frac{60 (\lambda_2 - \lambda_1) \cos L_1; \text{ if } C = 0}{60 (L_2 - L_1); \text{ otherwise}} \cos C$$

COMPUTING POSITION BY DEAD RECKONING

$$L_2 = \left(\frac{\Delta t \times GS \times \cos(TC)}{60} \right) + L_1$$

$$\text{If } TC = 90^\circ, 270^\circ \quad \lambda_2 = \lambda_1 - \left(\frac{\Delta t \times GS \times \sin(TC)}{60 \cos L_1} \right)$$

Otherwise:

$$\lambda_2 = \lambda_1 - \frac{180}{\pi} \left[\frac{\tan(TC) \times (\ln \tan(45 + 1/2 L_2) - \ln \tan(45 + 1/2 L_1))}{\cos L_1} \right]$$

NOTE: The flightpath may not cross the North Pole