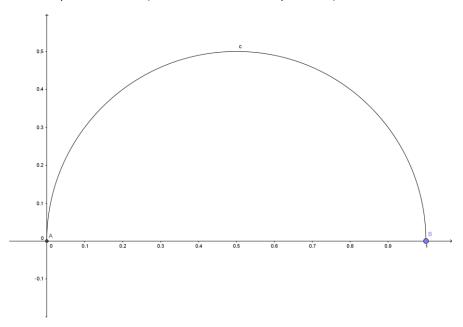
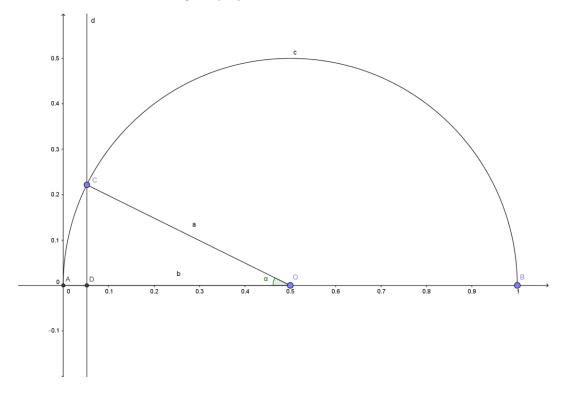
Determining Hc by graphical use of the all-haversine formula

Triggered by the worksheet for graphical sight reduction on Erik de Man's nautical pages [http://www.siranah.de/html/sail008h.htm] I set out to find if it would be possible to see if it could be done for the all haversine formula also.

I came up with a circle (or semi-circle for compactness) between 0 and 1.

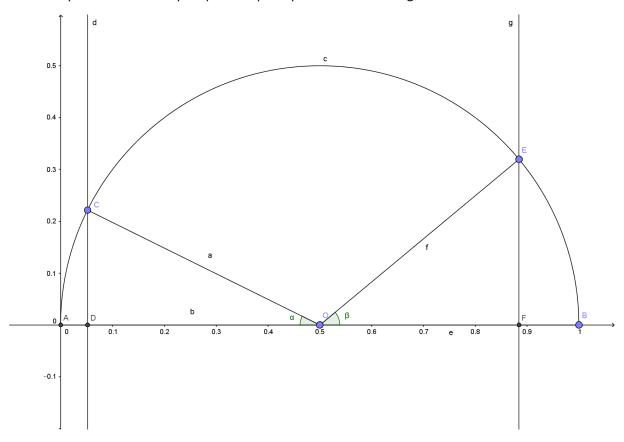


When a line is drawn from the center of the (semi-)circle at angle of α as the included angle of AOC, the distance AD with D being the projection of C on the x-axis is the haversine of α .



Can this be used to model the formula

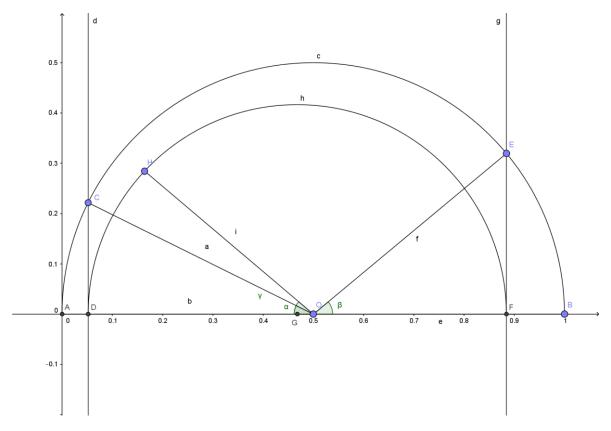
I think so. As the total distance between A and B is 1 (by definition) and we take $\alpha = |B - Dec|$, it is then also possible to define β as |B + Dec| and put it in the same figure.



In this figure AD = hav(|B - Dec|), FB = hav(|B + Dec|) and thus

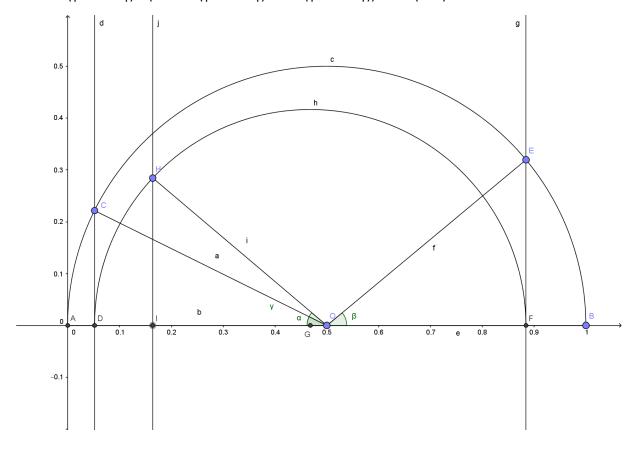
$$DF = (1 - hav (|B - Dec|) - hav (|B + Dec|)$$

Hav (LHA) is then constructed by drawing a new semi-circle between D and F. From the center G of this semi-circle a line GH is drawn so that the included angle γ in DGH equals LHA.



With I being the projection of H on the x-axis and DF being (1 - hav (|B - Dec|) - hav (|B + Dec|), DI becomes (1 - hav (|B - Dec|) - hav (|B + Dec|)) * hav (LHA) and

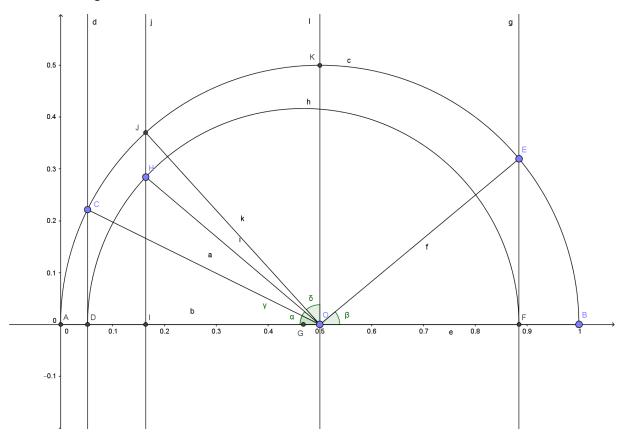
AI = hav(|B - Dec|) + (1 - hav(|B - Dec|) - hav(|B + Dec|)) * hav(LHA)



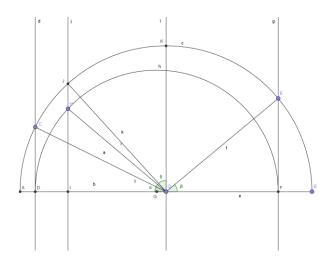
We then complete the determination of the zenith distance ZD, knowing

$$Hav(ZD) = hav(|B - Dec|) + (1 - hav(|B - Dec|) - hav(|B + Dec|)) * hav(LHA)$$

We can do this because we can see from the above hav (ZD) can be found by drawing a line from center C to a point J on the semi-circle AB such that the angle AOJ is the zenith distance. Hc being 90° - ZD means angle δ included in JOK is Hc.



As AB equals 1 by definition, it really isn't necessary to draw an axis with values. One could just start by drawing a line between to arbitrary points on an empty piece of paper and proceed from there.



Determining azimuth by graphical use of the all-haversine formula

Next up was the azimuth angle Zn. From rewriting the spherical law of cosines into an all haversine formula as has been done for Hc (ZD really) I found

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Hav (Dec) = hav (|B - ZD|) + (1 - hav (|B - ZD|) - hav (|B + ZD|)) * hav (Zn)
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So this can be modelled in the same way as Hc above, δ being Dec, γ being azimuth and α and β being hav (|B - ZD|) and hav (|B + ZD|) respectively.