

The cleared lunar distance is used to determine what GMT that distance corresponds to. The *Nautical Almanac* listed the lunar distances for the moon and various objects at three-hour intervals. The cleared distance would lie within one of those intervals.

The basic idea is to use interpolation to find the time corresponding to the cleared distance.

If

D is the angular difference between the tabulated distances which bracket your cleared distance: $dd^{\circ}mm'ss''_{UTC_i}$ and $dd^{\circ}mm'ss''_{UTC_i+3}$

and

d is the angular difference between the earlier tabulated distance and your cleared distance: $dd^{\circ}mm'ss''_{UTC_i}$ and $dd^{\circ}mm'ss''_{UTC_i+t}$

and

t is the yet unknown time interval hh:mm:ss between the earlier tabulated distance UTC and your observation moment: UTC_i and UTC_{i+t}

then:

$$\frac{D}{d} = \frac{3 \text{ [hours]}}{t}$$

or,

$$t \text{ [hours]} = 3 \text{ [hours]} \cdot \frac{d}{D}$$

or,

$$t \text{ [seconds]} = 10800 \text{ [seconds]} \cdot \frac{d}{D}$$

To simplify this calculation the "*proportional logarithm*" of time **t** as being the common log of 10800 [seconds] minus the common log of t [seconds] was introduced in the "*Tables Requisite*".

Because

$$D \cdot t = 10800 \cdot d$$

we can write:

$$\log D + \log t = \log 10800 + \log d$$

or,

$$\log t = \log 10800 + \log d - \log D$$

or, (subtracting each term from log of 10800 [seconds]):

$$\begin{aligned} & (\log 10800 - \log t) = \\ & = (\log 10800 - \log 10800) + (\log 10800 - \log d) - (\log 10800 - \log D) \end{aligned}$$

or,

$$(\log 10800 - \log t) = (\log 10800 - \log d) - (\log 10800 - \log D)$$

This is therefore:

$$plog t = plog d - plog D$$

where *plog* is the *proportional logarithm* as defined above.

An example:

On 2015-Jan-01 the reduced and cleared lunar distance between the Moon and Jupiter was found to be equal to 83°.

Looking up the *Precomputed Lunar Distances* table for that date one finds that the angle (83°) fits within the following brackets:

12:00 UT, 84° 35'.2, PL 2620

15:00 UT, 82° 56'.8, PL 2628

D, the total change in the distance during the three-hour interval (the angle between the brackets), equals to

$$84^\circ 35.2' - 82^\circ 56.8' = 1^\circ 38.4'$$

Looking 1° 38.4' up in "*Tables Requisite*" (in the **h. m.** column) one finds:

$$\text{plog } \mathbf{D} = 2623$$

d is the angular difference between the first distance tabulated at 12:00 UT and the distance cleared for the yet unknown time of lunar sight:

$$\mathbf{d} = 84^\circ 35.2' - 83^\circ 00.0' = 1^\circ 35.2'$$

Looking 1° 35.2' up in "*Tables Requisite*" (in the **h. m.** column):

$$\text{plog } \mathbf{d} = 2766$$

The plog **t** is their difference:

$$\text{plog } \mathbf{t} = \text{plog } \mathbf{d} - \text{plog } \mathbf{D} = 2766 - 2623 = 143$$

Looking up 143 in "*Tables Requisite*" (in the **PL** column) falls between the tabulated values of 142 and 145, which correspond to 2^h 54.2^m and 2^h 54.1^m or 02:54:12 and 02:54:06 respectively.

The interpolated value of **t** is approximately 02:54:10.

Adding the time offset **t** of the lunar to the UTC of the first time bracket gives us the UTC of the lunar itself:

$$12:00:00 + 02:54:10 = 14:54:10$$