

generally,  $\sin H = \sin L \sin d + \cos L \cos d \cos t$

When body is on the meridian,

$$\sin(H+C) = \sin L \sin d + \cos L \cos d \quad (t=0, \cos t=1)$$

where  $C$  is the correction to be added to the ex-meridian altitude,

Subtract:  $\sin(H+C) - \sin H = \cos L \cos d (1 - \cos t)$

$$2 \cos \frac{H+C+H}{2} \sin \frac{H+C-H}{2} = \cos L \cos d \quad 2 \sin^2 \frac{t}{2}$$

$$\sin \frac{C}{2} = \sin^2 \frac{t}{2} \frac{\cos L \cos d}{\cos \frac{2H+C}{2}} = \left\{ C \ll 2H \right\} = \sin^2 \frac{t}{2} \frac{\cos L \cos d}{\cos H}$$

As  $C$  and  $t$  are small quantities, then

$$\frac{C}{2} = \left( \frac{t}{2} \right)^2 \frac{\cos L \cos d}{\cos H}, \text{ where } C \text{ and } t \text{ are in radians}$$

$$\boxed{C_{\text{rad}} = \frac{1}{2} (t_{\text{rad}})^2 \frac{\cos L \cos d}{\cos H}}$$

If you want  $C$  expressed in minutes of arc, then

$$C_{\text{rad}} = \frac{C_{\text{moa}}}{60} \cdot \frac{\pi}{180}$$

and  $t$  expressed in either degrees or minutes of time,

$$t_{\text{rad}} = \begin{cases} t_{\text{deg}} \cdot \frac{\pi}{180} \\ \frac{t_{\text{mot}}}{60} \cdot 15 \cdot \frac{\pi}{180} \end{cases}$$

Greg's formula:  $\frac{C_{\text{moa}}}{60} \cdot \frac{\pi}{180} = \frac{1}{2} \left( t_{\text{deg}} \frac{\pi}{180} \right)^2 \frac{\cos L \cos d}{\cos H}$

$$C_{\text{moa}} = \frac{1}{2} \frac{60 \pi}{180} (t_{\text{deg}})^2 \frac{\cos L \cos d}{\cos H} = \frac{\pi}{6} (t_{\text{deg}})^2 \frac{\cos L \cos d}{\cos H}$$

0.5236

Bowditch: On meridian,  $H = 90^\circ - (L-d)$ ,  $\cos H = \cos(90^\circ - (L-d)) = \sin(L-d)$

$$\frac{C_{\text{moa}}}{60} \cdot \frac{\pi}{180} = \frac{1}{2} \left( \frac{t_{\text{mot}}}{60} \cdot 15 \cdot \frac{\pi}{180} \right)^2 \frac{\cos L \cos d}{\sin(L-d)}$$

$$C_{\text{moa}} = \frac{1}{60} \cdot \frac{15^2}{2} \cdot \frac{\pi}{180} (t_{\text{mot}})^2 \cos L \cos d \csc(L-d)$$

1.9635