

or Motion of the Body (for 1 minute) = $15 \times \cos(\text{Latitude}) \times \cos(270 - \text{Azimuth}) - (\cos(\text{True Course} - \text{Azimuth}) \times \text{Groundspeed} \div 60)$

$$\text{Rhumb line} = .146 \left(\frac{\text{GS}}{100} \right)^2 (\sin \text{TC})(\tan \text{LAT})$$

or Rhumb Line = $0.146 \times (\text{Groundspeed} \div 100)^2 \times \sin(\text{True Course}) \times \tan(\text{Latitude})$

$$\text{Coriolis} = (.0265)(\text{GS})(\sin \text{LAT})$$

or Coriolis = $0.02625 \times \text{Groundspeed} \times \sin(\text{Latitude})$

$$\text{Coriolis} = \cos(90 - \text{TC} - \text{Zn})(.0265)(\text{GS})(\sin \text{LAT})$$

or Coriolis = $\cos(90 - \text{True Course} - \text{Azimuth}) \times 0.02625 \times \text{Groundspeed} \times \sin(\text{Latitude})$

$$\text{Coriolis/rhumb line} = [(.0265)(\text{GS})(\sin \text{LAT})] + \left[(.146) \left(\frac{\text{GS}}{100} \right)^2 (\sin \text{TC})(\tan \text{LAT}) \right]$$

or Coriolis = $0.02625 \times \text{Groundspeed} \times \sin(\text{Latitude}) + [0.146 \times (\text{Groundspeed} \div 100)^2 \times \sin(\text{True Course}) \times \tan(\text{Latitude})]$

Great Circle Planning

Variables

L_1 = Departure Latitude (N and W = +)

L_2 = Destination Latitude (S and E = -)

λ_1 = Departure Longitude

λ_2 = Destination Longitude

L_i = Intermediate Latitude

λ_i = Intermediate Longitude

H_i = Initial True Heading

D = Distance

H = Heading Angle

Δt = Time between positions

GS = Groundspeed

TC = True Course

$$D = 60 \cos^{-1}[(\sin L_1)(\sin L_2) + (\cos L_1)(\cos L_2)\cos(\lambda_2 - \lambda_1)]$$

Distance = $60 \times \arccos((\sin(\text{Departure Latitude}) \times \sin(\text{Destination Latitude})) + (\cos(\text{Departure Latitude}) \times \cos(\text{Destination Latitude}) \times \cos(\text{Destination Longitude} - \text{Departure Longitude})))$

$$H = \cos^{-1} \left[\frac{\sin L_2 - \sin L_1 \cos \left(\frac{D}{60} \right)}{\sin \left(\frac{D}{60} \right) \cos L_1} \right]$$

or Heading Angle = $\arccos((\sin(\text{Destination Latitude}) - \sin(\text{Departure Latitude}) \times \cos(\text{Distance} \div 60)) \div (\sin(\text{Distance} \div 60) \times \cos(\text{Departure Latitude})))$

$H_i = H \quad \sin(\lambda_2 - \lambda_1) < 0$

$H_i = 360 - H \quad \sin(\lambda_2 - \lambda_1) > 0$

This formula computes the latitude of L_i where λ_i intersects the great circle defined by (L_1, λ_1) and (L_2, λ_2) . This formula can be very useful when matching charts of different projections or scales.

$$L_i = \tan^{-1} \left[\frac{(\tan L_2)\sin(\lambda_i - \lambda_2) - (\tan L_1)\sin(\lambda_i - \lambda_1)}{\sin(\lambda_i - \lambda_2)} \right]$$

or Intermediate Latitude = $\text{atan}((\tan(\text{Destination Latitude}) \times \sin(\text{Intermediate Longitude} - \text{Departure Longitude})) - (\tan(\text{Departure Latitude}) \times \sin(\text{Intermediate Longitude} - \text{Destination Longitude}))) \div \sin(\text{Destination Longitude} - \text{Departure Longitude}))$

Computing Position By Dead Reckoning:

$$L_2 = \left(\frac{(\Delta t)(GS)(\cos TC)}{60} \right) + L_1$$

or DEST Latitude = (Elapsed Time \times Groundspeed \times cos(True Course)) \div 60 + Departure Latitude

$$\lambda_i = \lambda_2 - \left(\frac{(\Delta t)(GS)(\sin TC)}{60 \cos L_1} \right)$$

TC = 90°, 270°

or DEST Longitude = Departure Longitude - ((Elapsed Time \times Groundspeed \times sin(True Course)) \div (60 \times cos(Departure Latitude)))

Otherwise

$$\lambda_2 = \lambda_1 - \frac{180}{\pi} \{ (\tan TC)[L_n \tan(45 + \frac{1}{2}L_2)] - (L_n \tan(45 + \frac{1}{2}L_2)) \}$$

or DR Longitude = Departure Longitude - $(180 \div 3.14159) \times (\tan(\text{True Course}) \times \ln(\tan(45 + 0.5 \times \text{Destination Latitude})) - \ln(\tan(45 + 0.5 \times \text{Departure Latitude})))$

NOTE: The flightpath may not cross either pole.

For long distances, use formula below:

DR Latitude = $90.0 - \text{acos}(\sin(-\text{Departure Latitude}) \times \cos(\text{Distance} \div 60.0) + \cos(-\text{Departure Latitude}) \times \sin(\text{Distance} \div 60.0) \times \cos(\text{True Course}))$

DR Longitude = Departure Longitude \pm $\text{acos}((\cos(\text{Distance} \div 60.0) - \sin(-\text{DR Latitude}) \times \sin(-\text{Departure Latitude})) \div (\cos(-\text{DR Latitude}) \times \cos(-\text{Departure Latitude})))$

NOTE: Distance can be replaced with (Groundspeed \times Elapsed Time) where Elapsed Time is in hours.

Rhumb Line Planning

Variables

Δt = Time between positions

D = Rhumb line Distance

C = Rhumb line True Course

π = Pi (≈ 3.14159)

$$C = \tan^{-1} \left[\frac{\pi (\lambda_2 - \lambda_1)}{180 L_n \tan(45 + \frac{1}{2}L_2) - (L_n \tan(45 + \frac{1}{2}L_1))} \right]$$

or True Course = $\text{atan}((3.14159 \times (\text{Departure Longitude} - \text{Destination Longitude})) \div (180 \times \ln(\tan(45 + 0.5 \times \text{Destination Latitude})) - \ln(\tan(45 + 0.5 \times \text{Departure Latitude}))))$

$$D = 60(\lambda_2 - \lambda_1)\cos L_1$$

$$C = 0$$

or Distance = $60 \times (\text{Destination Longitude} - \text{Departure Longitude}) \times \cos(\text{Departure Latitude})$

$$D = \frac{60 (L_2 - L_1)}{\cos C}$$

$$C = 0$$